

Methane Dication: Planar but Not Square

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The doubly charged ion of methane (CH_4^{2+}) is of fundamental importance among gas-phase dications¹ and has been the subject of many experimental² and theoretical^{2d,3} studies. The highlight of the theoretical studies has been the demonstration that the methane dication is the simplest species containing a planar, tetracoordinate carbon atom. The best theoretical calculations to date^{3c,d} have indicated that CH_4^{2+} has an anti-van't Hoff square-planar (D_{4h}) geometry, in contrast to the tetrahedral (T_d) structure of neutral methane, and this conclusion has been widely accepted.

We show here, through calculations of the geometry at much higher levels of theory than those previously employed, that the methane dication is planar but distinctly not square. The square-planar (D_{4h}) geometry of CH_4^{2+} does not in fact correspond to a minimum on the potential energy surface at the higher levels of theory. The preferred structure of CH_4^{2+} is found to be planar with C_{2v} (rather than D_{4h}) symmetry and is characterized by two long and two short C-H bonds and a narrow HCH bond angle between the two longer C-H bonds. It thus resembles a complex between the methylene dication (CH_2^{2+}) and a hydrogen molecule.

Our initial ab initio calculations^{4,5} involved geometry optimizations of C_{2v} (**1**) and D_{4h} (**2**) structures of CH_4^{2+} (see Figure 1) with three different basis sets, namely 6-31G*, 6-31G**, and 6-311G**, and with electron correlation incorporated via Møller-Plesset perturbation theory terminated at second (MP2)-, third (MP3)-, or fourth (MP4)-order,⁸ via configuration interaction calculations with single and double substitutions (CISD),⁸ or via full-valence CASSCF theory.⁹ A selection of optimized geometries is shown in Table I and corresponding total and relative energies in Table II.¹⁰

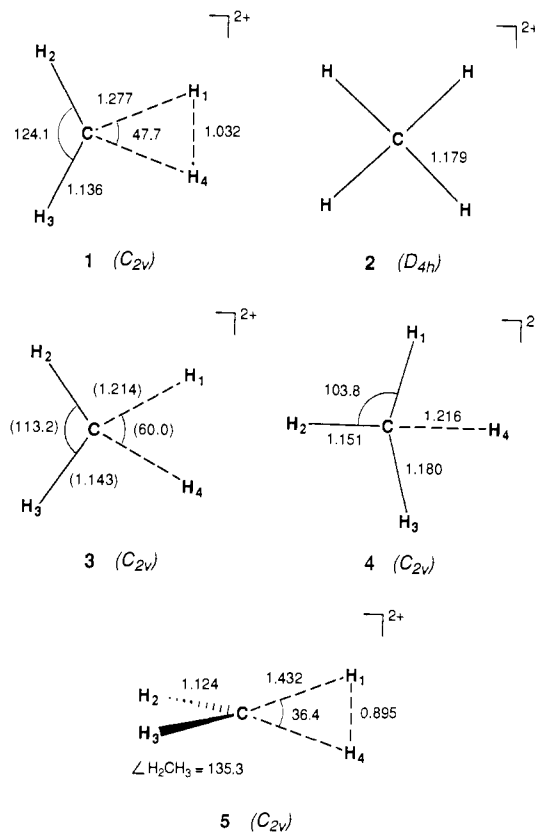


Figure 1. Optimized structures (MP3/6-311G** values, with MP2/6-31G* values in parentheses) for methane dication.

With the (smallest) 6-31G* basis set, both C_{2v} (**1**) and D_{4h} (**2**) structures of methane dication are found to be stable minima (confirmed by frequency calculations at both Hartree-Fock and MP2 levels) on the potential energy surface. The C_{2v} structure (**1**) resembles a complex between the CH_2^{2+} dication and a hydrogen molecule and thus is strikingly different from the D_{4h} form (**2**), but the energies of **1** and **2** are very similar (Table II). At the MP2/6-31G* level, we have located a transition structure **3** (Figure 1) connecting **1** and **2**, but it lies just 1 kJ mol⁻¹ above **1**.

Calculations with the inclusion of p polarization functions on hydrogen (6-31G* \rightarrow 6-31G**) favor strongly the C_{2v} structure (Table II). Although the D_{4h} geometry (**2**) is a true minimum at the HF/6-31G** level, at the MP2 level it corresponds to a second-order saddle point (as shown by a degenerate pair of imaginary frequencies). Rearrangement of **2** (at MP2/6-31G**) along the normal coordinates representing these frequencies leads without a barrier to **1**.

The results for the triple- ζ valence 6-311G** basis set confirm the strong preference for the C_{2v} structure **1** over the D_{4h} form **2**. With this basis set, the D_{4h} structure **2** is no longer a local minimum on the CH_4^{2+} potential energy surface: it represents a second-order saddle point at both Hartree-Fock and MP2 levels. The preferred planar C_{2v} structure **1** is characterized by the following harmonic vibrational frequencies (MP2/6-311G**, scaled¹¹ by 0.93): 906 (a_1), 942 (b_2), 1022 (a_2), 1105 (b_1), 1426 (a_1), 1608 (b_2), 2163 (a_1), 2570 (a_1), and 2671 (b_2) cm⁻¹. At our best level of optimization (MP3/6-311G**), **1** has a bond angle H_1CH_2 of 47.7° and bond lengths C-H₁ and C-H₂ of 1.277 and 1.136 Å, respectively. The $\text{H}_1\cdots\text{H}_4$ distance is 1.032 Å (Figure 1).

Results at still higher levels of theory (Table II) indicate that there is little change in the relative energy in going from the 6-311G** to the 6-311G(2d,2p) basis, while inclusion of diffuse functions and f polarization functions reduces the relative energy by about 3 kJ mol⁻¹. It is evident that all calculations using basis

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Table I. Optimized Geometries for the Planar C_{2v} (1) and D_{4h} (2) Structures of CH_4^{2+}

	C_{2v} (1)			D_{4h} (2)	
	$r(C-H_1)$	$r(C-H_2)$	$r(H_1-H_4)^a$	$\angle H_1CH_4$	$\angle H_2CH_3$
HF/6-31G*	1.238	1.119	1.000	47.7	122.2
MP2/6-31G*	1.232	1.136	1.085	52.3	118.8
HF/6-31G**	1.256	1.119	0.988	46.3	123.8
MP2/6-31G**	1.250	1.127	1.022	48.3	122.7
HF/6-311G**	1.275	1.120	0.995	45.9	124.8
MP2/6-311G**	1.268	1.134	1.046	48.7	123.2
MP3/6-311G**	1.277	1.136	1.032	47.7	124.1
CISD/6-311G**	1.280	1.134	1.022	47.0	124.5
CASSCF/6-311G**	1.304	1.143	1.002	45.2	126.2

^aNonindependent parameter, included for completeness.

Table II. Calculated Total Energies (hartrees) and Relative Energies (kJ mol⁻¹) for the Planar C_{2v} (1) and D_{4h} (2) Structures of CH_4^{2+} ^a

	total energies ^b		relative energies	
	C_{2v} (1)	D_{4h} (2)	C_{2v} (1)	D_{4h} (2)
HF/6-31G*	-39.04744 (0)	-39.04694 (0)	0	1.3
MP2/6-31G*	-39.15268 (0)	-39.15491 (0)	0	-5.9
MP3/6-31G*	-39.16597	-39.16805	0	-5.5
MP4/6-31G*	-39.17050	-39.17245	0	-5.1
CISD/6-31G*	-39.16657	-39.16849	0	-5.0
CASSCF/6-31G*	-39.12776	-39.12729	0	1.2
HF/6-31G**	-39.06549 (0)	-39.05821 (0)	0	19.1
MP2/6-31G**	-39.18474 (0)	-39.17961 (2)	0	13.5
HF/6-311G**	-39.07680 (0)	-39.06668 (2)	0	26.6
MP2/6-311G**	-39.21196 (0)	-39.20642 (2)	0	14.5
MP3/6-311G**	-39.21293	-39.20668	0	16.4
CISD/6-311G**	-39.21285	-39.20590	0	18.2
CASSCF/6-311G**	-39.15928	-39.14844	0	28.5
MP4/6-311G(2d,2p) ^c	-39.22505	-39.21882	0	16.4
ST4CCD/6-311G(2d,2p) ^c	-39.22646	-39.22012	0	16.6
HF/6-311+G(2df,2p) ^c	-39.07944	-39.06941	0	26.3
MP2/6-311+G(2df,2p) ^c	-39.21046	-39.20589	0	12.0
MP3/6-311+G(2df,2p) ^c	-39.22948	-39.22471	0	12.5
MP4/6-311+G(2df,2p) ^c	-39.23504	-39.23007	0	13.0
CCD/6-311+G(2df,2p) ^c	-39.23244	-39.22703	0	14.2
ST4CCD/6-311+G(2df,2p) ^c	-39.23640	-39.23129	0	13.4

^aGeometries fully optimized at the level specified, unless otherwise noted. ^bNumber of imaginary frequencies in parentheses. ^cMP3/6-311G** optimized structures.

sets larger than 6-31G* clearly favor the C_{2v} structure **1** over the D_{4h} structure **2**. At our best level of theory, which involves large basis set coupled-cluster calculations at the ST4CCD level¹² (ST4CCD/6-311 + G(2df,2p)), the C_{2v} structure **1** is more stable than the D_{4h} structure **2** by 13 kJ mol⁻¹. Zero-point vibrational correction leads to a final prediction of 4 kJ mol⁻¹.¹³

As noted earlier, the C_{2v} structure **1** can be regarded as a complex of the methylene dication and a hydrogen molecule. The calculated stabilization energy associated with this three-center two-electron (3c-2e) donor-acceptor interaction^{14,15} is 381 kJ mol⁻¹.¹⁶ A similar donor-acceptor complex has been reported¹⁷

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for the second-row analogue SiH₄²⁺. We note also that 3c-2e stabilization is a common structural feature in other carbocations: for example, CH₆²⁺,¹⁸ C₂H₆²⁺,¹⁹ C₂H₈²⁺,¹⁹ and C₃H₈²⁺.^{20,21}

We have located a transition structure **4** for hydrogen scrambling in **1**, but its energy is only 4 kJ mol⁻¹ above **1**. Hydrogen scrambling in **1** should, therefore, be very rapid, and the experimental identification of nonequivalent hydrogens in the planar C_{2v} structure will not be straightforward.

The perpendicular C_{2v} structure **5** lies 54 kJ mol⁻¹ higher than **1** and corresponds to a rotational transition structure. It represents a weaker complex than the planar form **1**, as reflected by the longer C-H₁ bond (1.432 Å) and shorter H₁-H₄ distance (0.895 Å). The preference for the planar structure **1** can be rationalized in terms of the back-donation from the pseudo- π orbital of the CH₂²⁺ group in **1** to the σ^* orbital of H₂.

In conclusion, we have confirmed that the methane dication prefers a planar anti-van't Hoff geometry. We have shown, however, that it has C_{2v} symmetry rather than the previously accepted square-planar D_{4h} structure.

Acknowledgment. We gratefully acknowledge a generous allocation of computer time on the Fujitsu FACOM VP-100 of the Australian National University Supercomputer Facility.

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